

Probability (cont.); repeat end of last lecture to clarify:

Probability we usually use in psychology is probability<sub>2</sub>: Proportion in a class, percentage, relative frequency of events or properties; a decimal value  $0 \leq p \leq 1$  closed interval; "certainty" = ( $p = 1$ ), but not conversely

Object language. Properties of physical objects or events in a domain (genetics, chemistry, psychology, economics)  
19th century, John Venn; and Ellis defined by relative frequency

Kolmogoroff, axiomatized probability calculus.  $P$  not *defined* by reference to relative frequency. Only 3 postulates about probability numbers. All abstract. Have to coordinate linkages of the  $p$ -numbers with empirical proportions. I don't know how to do that.

Popper. Probability is a *propensity* (= tendency, disposition), and a formal axiom system. Thinks you need more axioms than 3.

Fisher is a frequentist, but not the Mises-Reichenbach kind. Introduce  $\pi$  by axiom, then *prove* it relates to a frequency.

Psychology students think frequency is the only kind of probability there is, from way statistics is taught. Another kind of probability (life, law courts, even science) doesn't *look* like a relative frequency.

Historical fact (e.g., Katyn massacre) on evidence, doesn't look like any kind of frequency.

Kaspar Hauser son of a prince? How express a probability of that as a frequency?  
Only one such person.

Wegener theory of continental drift. If no other planets exist, still meaningful to say "Wegener's theory is probable on the evidence."

*Facts* may be statistical or not. But that doesn't make the evidentiary relation *between* facts and theory statistical.

Schizophrenia is a neurological disorder, on the evidence  $p(T/F)$  has no algorithm to get a  $p$ -number. Bayesian subjectivists *extract* a  $p$ -number by forcing people to bet. It works.

But those subjective betting odds are not reached by computing a frequency.

Start with Carnap's probability<sub>1</sub> and probability<sub>2</sub> *prima facie* distinction; *then* inquire whether they can be identified, or how related if distinct. Probability<sub>1</sub> is about relation between beliefs, statements, propositions—rather than relations between events or properties of physical events

Can always avoid facts (Flat Earth Society)

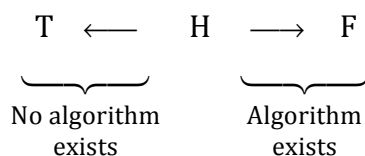
Cardinal Newman's book *Grammar of Assent* is great on probability<sub>1</sub>

Example: Evidence that Hauptman killed Lindbergh baby [passout]

Example: Snyder's genetics text (pre-1953) that genes are located on chromosomes [passout]

Any juror has to estimate probability<sub>1</sub> without algorithm

Scientific theories are probability<sub>1</sub> on evidence (Piaget, Darwin, Freud, Big Bang) not numerified by an algorithm



probability<sub>1</sub> called “logical probability”

Carnap worked on a probability<sub>1</sub> algorithm

Most don't think it worked

Perfect ideal language of state-descriptives

“Principle of Indifference” or “Principle of Insufficient Reason” applied to state descriptions can give an algorithm [Grover Maxwell story on state descriptions]

Probability<sub>1</sub> and probability<sub>2</sub> prima facie different, and we need both kinds

“Probability is the guide of life” (Bishop Butler)

Query: Yet how are they basically the same? How come same term used for both (in most languages)?

[Randomness of von Mises collectives is called “Principle of Impossibility of a Gambling System”]

von Mises said shouldn't use term ‘probability’ at all, for probability<sub>1</sub>.

Reichenbach said only one meaning, limit of relative frequency, for both kinds.

Hard to defend. Example: Probability<sub>1</sub> of scientific theories would really be relative frequency of truth for theories having certain properties.

Some of our most fundamental concepts are fuzzy. Example: Probability; causality.

Why one word? Carnap: “Fair betting odds.” Subjective Bayesians even *define* probability that way.

If truth-frequency in long run doesn't match a purported probability<sub>1</sub> algorithm, algorithm is defective. Example: 1000 murder cases where truth is known; a jury algorithm for evaluating evidence should agree; otherwise it's no good however logically plausible it seems. In that sense relative frequency has a basic status in all probability concepts. So identity theorists like Reichenbach have a point.

de Finetti, Savage “Dutch Book” argument.

Conceptually distinct, yet probability<sub>2</sub> and probability<sub>1</sub> should tend to agree in long run.

#### Clinical vs statistical prediction

Autobiographical note: My Freudian interests vs 1938–1945 Minnesota department (anti-Freudian, behaviorist, statistical)

Examples: Law school admissions; criminal parole; suicide risk; EST or pills.  
Serious matters. (“Help,” “change” presupposes prediction.)

Doing nothing is a form of action, a decision, based on estimate of effects of options. All such predictions are probabilistic and will remain so. Some physical sciences also stochastic (e.g., meteorology).

Meteorology predictions only 15% better than “persistence” prediction

Closed outcome set: Defined predictive task

Almost all such judgments are made by “informal” method (reflect, discuss, vote, or chief decide).  
On any given day in USA, 99.9% of all decisions about human behavior are made informally.

Kind of data vs mode of combining them

Other way: Once data encoded, a mechanical way, algorithm, puts data together → prediction.  
“Actuarial” “statistical” But also can make a mechanical rule non-actuarially (armchair)